

A Global Multi-Decadal Oscillation

Timothy DelSole

George Mason University, Fairfax, Va and
Center for Ocean-Land-Atmosphere Studies, Calverton, MD

October 11, 2009

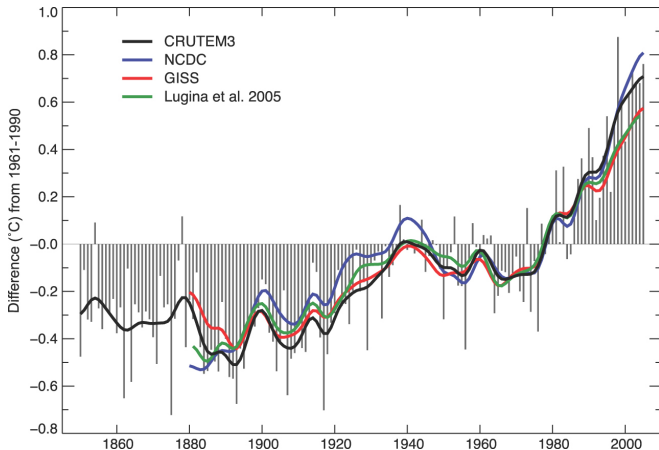
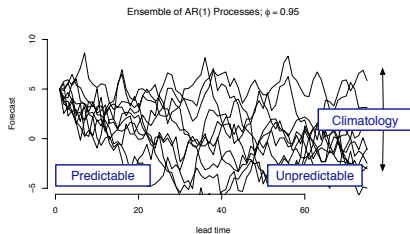


Figure: Annual anomalies of global land-surface temperature (from IPCC-AR4; figure 3.1)

Questions

- ▶ How much variability is forced?
- ▶ How much variability is due to internal mechanisms?
- ▶ How much of the internal variability is predictable?

Definition of Predictability

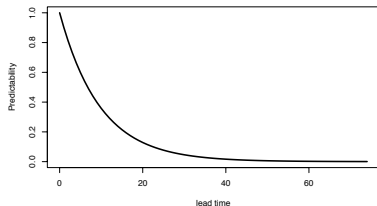


Measure of Predictability

$$P = \frac{\sigma_c^2 - \sigma_f^2}{\sigma_c^2}$$

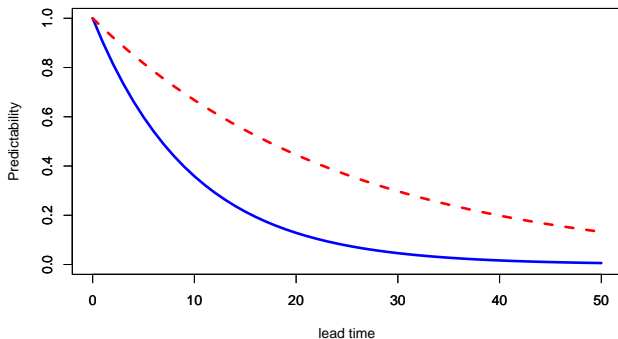
σ_f^2 : Variance of forecast.

σ_c^2 : Variance of climatology.



Can predictability be characterized in a way that is independent of lead time?

Average Predictability Time (APT)



APT = integral of 2P over all lead times

$$APT = 2 \int_0^{\infty} \left(\frac{\sigma_c^2 - \sigma_f^2}{\sigma_c^2} \right) d\tau$$

Optimize APT

Find projection of the data that maximizes APT. Solution:

$$\left(2 \int_0^{\infty} \boldsymbol{\Sigma}_c - \boldsymbol{\Sigma}_f d\tau \right) \mathbf{q} = \lambda \boldsymbol{\Sigma}_c \mathbf{q}$$

where $\boldsymbol{\Sigma}_f$ and $\boldsymbol{\Sigma}_c$ are the forecast and climatological covariance matrices.

- ▶ Eigenvalue λ gives the APT.
- ▶ Eigenvectors \mathbf{q} are projection vectors for generating time series.
- ▶ Resulting time series are uncorrelated in time.
- ▶ Each projection vector is associated with physical pattern $\mathbf{p} = \boldsymbol{\Sigma}_c \mathbf{q}$.
- ▶ Physical pattern \mathbf{p} is called a **predictable component**.
- ▶ Product of $\mathbf{p} *$ (time series), summed over all components, recovers original time series.

Estimating APT With Only One Ensemble Member

- ▶ Project data onto M principal components $\mathbf{r}(t)$.
- ▶ Construct multivariate linear regression model

$$\mathbf{r}(t + \tau) = \mathbf{L}_\tau \mathbf{r}(t) + \boldsymbol{\epsilon}(t).$$

- ▶ Determine forecast variance from standard regression formula

$$\boldsymbol{\Sigma}_f = \boldsymbol{\Sigma}_r - \mathbf{L}_\tau \boldsymbol{\Sigma}_r \mathbf{L}_\tau^T.$$

where $\boldsymbol{\Sigma}_r$ is the covariance matrix of \mathbf{r} .

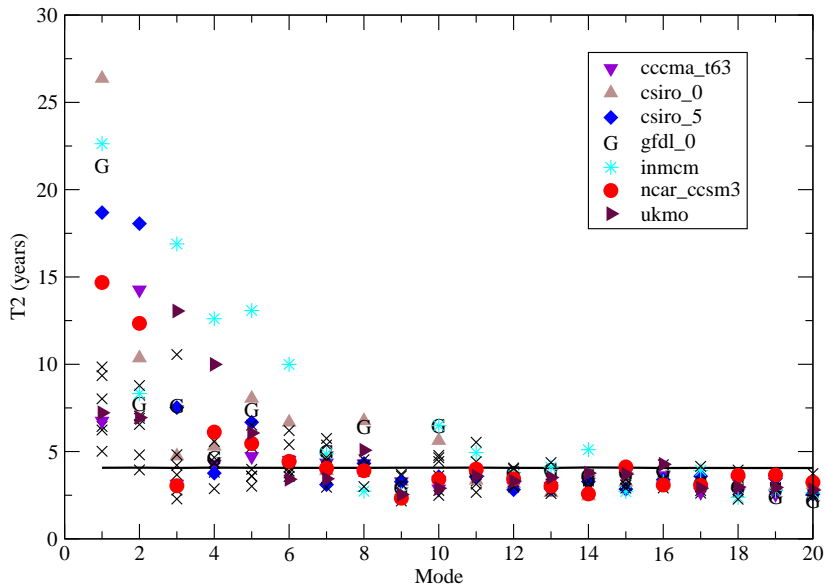
- ▶ Optimize APT using $\boldsymbol{\Sigma}_f$ defined above and $\boldsymbol{\Sigma}_c = \boldsymbol{\Sigma}_r$.
- ▶ **Limitations:** May miss non-linear predictability.

Optimize APT in Unforced Climate Runs

- ▶ Last 300 years of PICNTRL are used (13-16 models).
- ▶ Model grids interpolated onto HADCRUT3 grid.
- ▶ Annual averaged sea surface temperature.
- ▶ Each model's climatology subtracted out.
- ▶ All runs pooled to compute “total EOF” and “total APT.”
- ▶ Effective length = 4500 years.
- ▶ 40 EOF truncation, 20-year maximum lag for APT.
- ▶ IAP, GISS-EH dropped due to significantly different variability.
- ▶ **No Detrending**
- ▶ Test hypothesis that time series is white noise when sampled every 2 years (use Monte Carlo to estimate sampling distribution of APT).

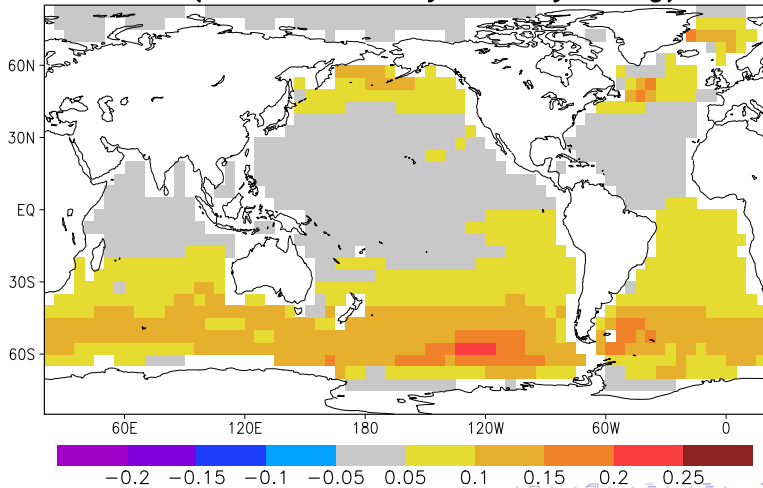
APT Values for Individual Models

T2 values for apt for tos.ann.terp.glo
nyrs=300, picntrl, ntrun=40, lagmx=20



Leading Predictable Component (The “Global Multidecadal Oscillation”)

tos.ann.terp.glo apt(5.92yr) Mode-1
(40EOFs; 300yrs; 20yr Lag)



10-year average

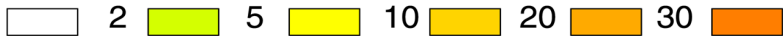
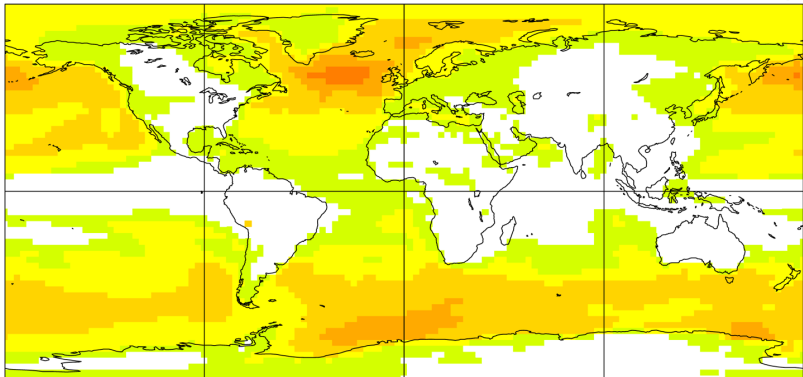
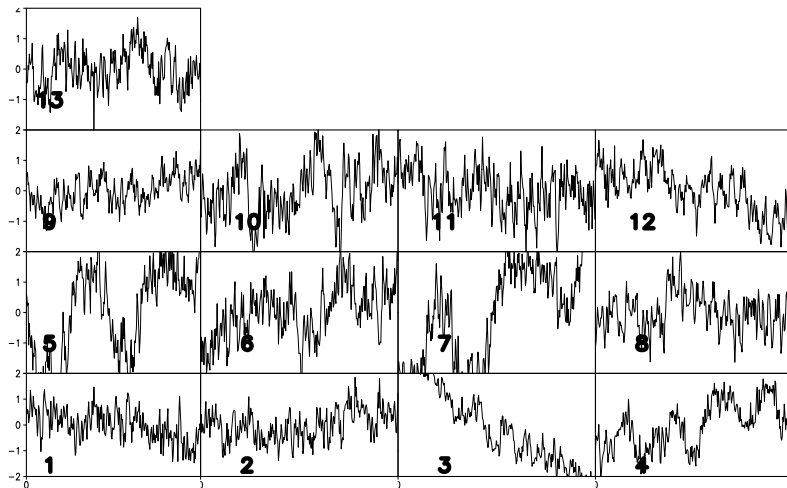


Figure: Estimated percentage of variance of 10-year mean temperature that is potentially predictable (Boer and Lambert 2008).

Leading Predictable Component



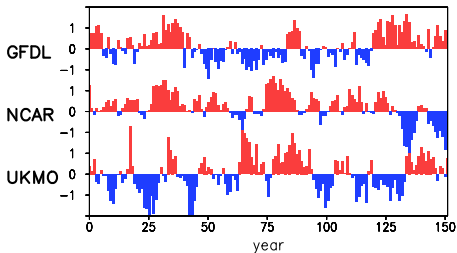
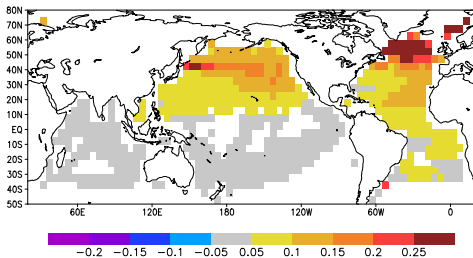
Horizontal axes: time (0-300 years); Vertical axes: amplitude (-2,2)

Models and the APT of the Most Predictable Component

Index	Model	APT-1D
1	cccma_cgcm3_1	6.4
2	cccma_cgcm3_1_t63	6.7
3	csiro_mk3_0	26.4
4	csiro_mk3_5	18.7
5	gfdl_cm2_0	21.3
6	gfdl_cm2_1	9.8
7	inmcm3_0	22.6
8	ipsl_cm4	6.2
9	miroc3_2_medres	8
10	miub_echo_g	9.3
11	mri_cgcm2_3_2a	5
12	ncar_ccsm3_0	14.7
13	ukmo_hadcm3	7.2

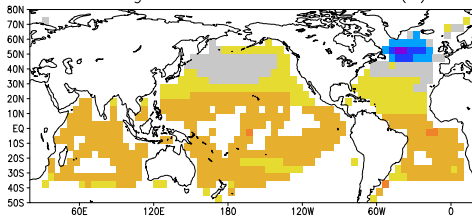
Optimize APT on “Well-Observed” Grid

tos.ann.terp.mis apt(5.07yr) Mode-1
(40EOFs; 300yrs; 20yr Lag)

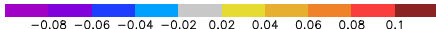
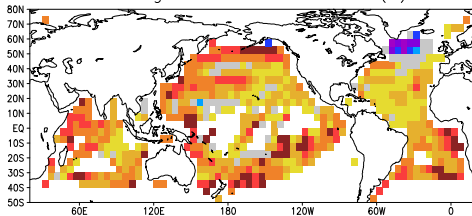


Estimates of the Forced Response

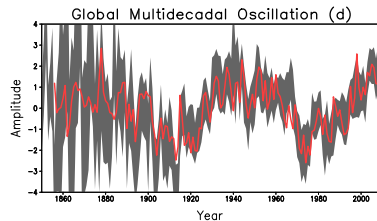
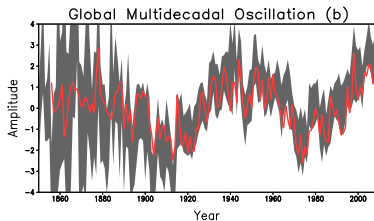
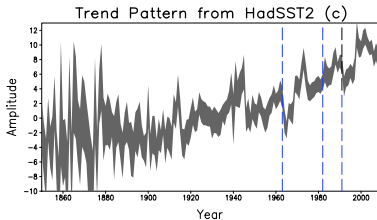
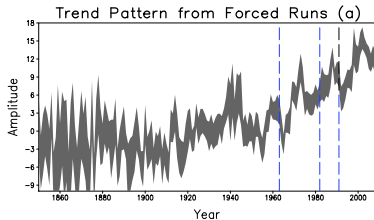
Average Trend in Forced Runs (a)



Average Trend in HadSST2 (b)



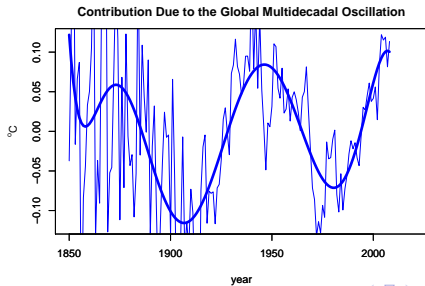
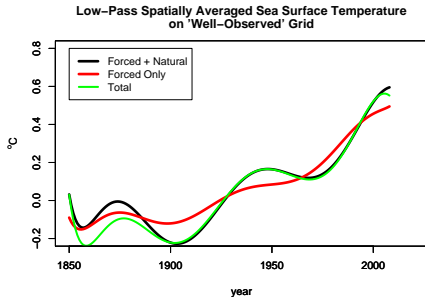
Fingerprint Analysis



red curves: annual average Atlantic Multidecadal Oscillation Index

blue lines: Mt. Agung (1961), El Chichon (1982), Mt. Pinatubo (1991)

Global Average Temperature



Summary

- ▶ We have introduced a new method for seamlessly diagnosing predictability on multiple time scales.
- ▶ The most predictable component in the IPCC-control runs (the “GMO”) is statistically significant in all models.
- ▶ The GMO is of single sign and global in spatial extent.
- ▶ Decomposing observed SST into forced and GMO components:
Forced component: multidecadal trend plus volcanic cooling.
GMO component: strongly correlated with AMO.
- ▶ GMO component explains 0.1° fluctuations in low-pass, global average SST (on “well observed grid”), including
 - ▶ all the cooling between 1940-1970.
 - ▶ half of the warming in the past 25 years.
- ▶ The GMO component is currently at a peak and may decay in the next 20 years, leading to little or no warming in the next 20 years.